

# Minimization of NBTI Performance Degradation Using Internal Node Control

David R. Bild<sup>†</sup>, Gregory E. Bok<sup>‡</sup>, and Robert P. Dick<sup>†</sup>

<sup>†</sup>Department of EECS  
University of Michigan  
Ann Arbor, MI 48109, USA

<sup>‡</sup>Nico Trading  
311 S. Wacker Drive, Suite 900  
Chicago, IL 60606, USA

This work was performed while the authors were with the Department of Electrical Engineering and Computer Science, Northwestern University, Evanston IL 60208, USA.

April 21, 2009

# Outline

1. Introduction
2. Background
  - NBTI
  - Internal Node Control
3. Optimal Formulation
  - MILP
  - Experimental Results
4. Heuristic
  - Algorithm
  - Experimental Results

# Outline

1. Introduction
2. Background
3. Optimal Formulation
4. Heuristic

# What is NBTI

## Negative Bias Temperature Instability

- Breakdown of Si-H bonds which leads to increased threshold voltage
- Reduction in transconductance and thus switching speed
- Significant for PMOS transistors under negative bias
- Partially recovers when negative bias is removed

# Contributions

## Internal Node Control

- Input Vector Control (IVC) – control the primary inputs
- Internal Node Control (INC) – extend control to internal nodes

## Contributions

- Analyzed the potential benefit of using INC to reduce static NBTI degradation
- Developed a fast, near-optimal heuristic for the application of INC

## Results

- INC – Average 26.7% improvement relative to IVC only
- INC+IVC – Average 51.3% decrease in NBTI-induced delay

# Outline

1. Introduction
2. Background
3. Optimal Formulation
4. Heuristic

# Section outline

## 2. Background

NBTI

Internal Node Control

# Physical Process

## Reaction-Diffusion Model

- Reaction: Electric-field dependent disassociation of Si-H bonds at Si/SiO<sub>2</sub> interface
- Creation of interface traps, dangling bonds, oxide charges
- Diffusion: H or H<sub>2</sub> diffuses into the oxide

## Recovery Effect

- Stress is removed
- Hydrogen diffuses back towards the interface
- Re-bonds with Si



# Analytical Models

## Types of Stress

- Static: Continuously applied stress (e.g., idle functional unit)
- Dynamic: Alternating stress and recovery (e.g., operating functional unit)

## Models

- Cycle-based, transistor-level simulation is too slow
- Analytical models have been developed
- Overestimate degradation for static stress

## Our Model

- Aggregate, long-term effect of static stress
- Assume 10% increase in delay after 10 years (Paul et. al)

# Managing NBTI

## Compensating Techniques

- Guardbanding
- Gate sizing
- $V_{dd}$  tuning
- $V_{th}$  tuning

## Mitigating Techniques

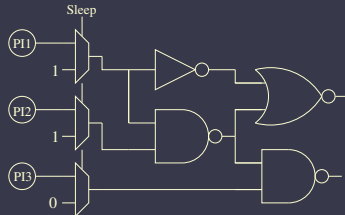
- Power gating
- Clock gating
- Input Vector Control (IVC)

# Input Vector Control

Wang et al. in DATE 2006

- In sleep mode, set the primary inputs to minimize the impact on circuit delay
- Implement with MUXes, scan-chains, or modified registers
- Con: Limited effectiveness on deeper levels of logic

## Example



## Section outline

### 2. Background

NBTI

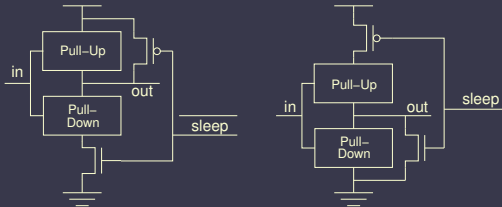
Internal Node Control

# INC Implementation

## Power Minimization

- Proposed by Abdollahi, Fallah, and Pedram
- Add INC to some internal gates
- Force the output value with sleep signal

## INC Implementation

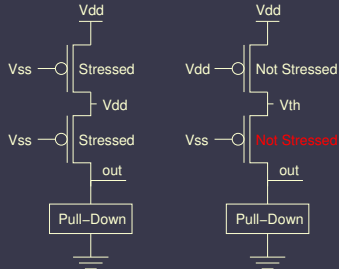


# Potential for NBTI

## Inverting Logic

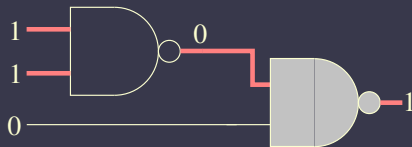
- All inputs high leads to low output
- Would have to force all outputs high to eliminate all stress
- Focus on critical path transistors instead

## NOR Gate Stack

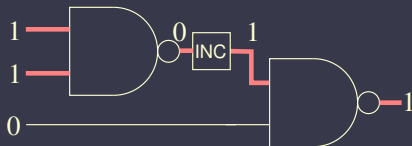


# Example Insertion Scenario I

Inline

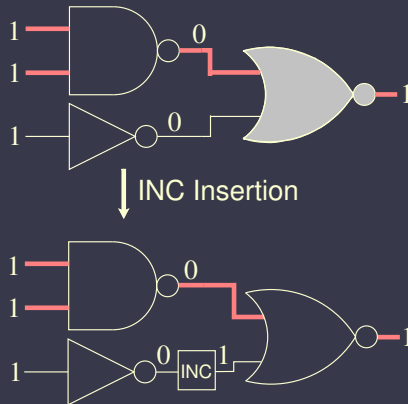


↓ INC Insertion



## Example Insertion Scenario II

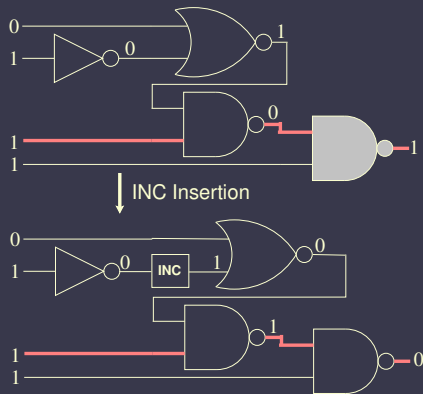
### NOR Stack





## Example Insertion Scenario III

### Offpath



# Formal Problem Definition

## Given

- A combinational circuit
- For each gate, the basic delay, INC delay, and NBTI delay

## Find

- Input vector
- INC insertion points

## Such That

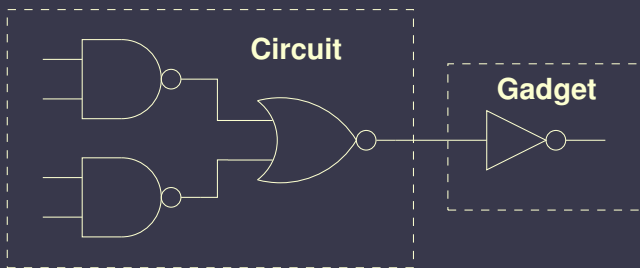
- The critical path delay (post-NBTI) is minimized

# Complexity

## $\mathcal{NP}$ -complete

- The problem is in  $\mathcal{NP}$  by polynomial-time checking
- Prove  $\mathcal{NP}$ -hard via reduction from circuit-SAT

## Circuit-SAT Reduction



# Outline

1. Introduction
2. Background
3. Optimal Formulation
4. Heuristic

# Section outline

## 3. Optimal Formulation

MILP

Experimental Results

# Optimal Formulation

## MILP

- MILP formulation
- Solved using Symphony open-source solver

## Gate Library

- 7 gate library in 65 nm
- Characterized timing (for INC and non-INC) using SPICE
- Verified against TSMC library

## Benchmarks

- ISCAS85 benchmarks
- Synthesized using Synopsys Design Compiler

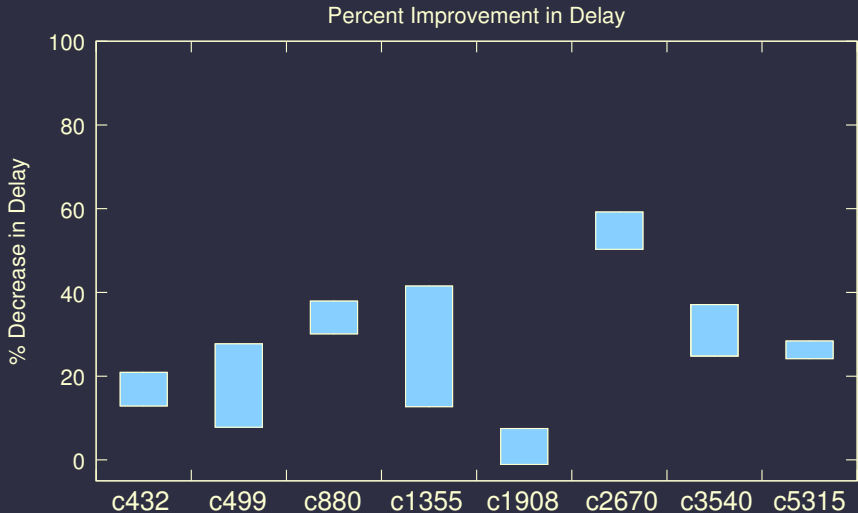
# Section outline

## 3. Optimal Formulation

MILP

Experimental Results

# Optimal Experimental Results I





# Optimal Experimental Results II

## Summary

- 26.7% average improvement relative to optimal IVC
- 51.3% average improvement relative to average IVC

# Outline

1. Introduction
2. Background
3. Optimal Formulation
4. Heuristic

## Section outline

### 4. Heuristic

Algorithm

Experimental Results

# Motivation

## Complexity

- Problem is  $\mathcal{NP}$ -hard
- For small benchmarks, can only generate upper and lower bounds on optimal

## Heuristic Overview

- Linear-time
- Tree-partitioning and dynamic programming
- Based on work by Cheng, Chen, and Wong

# Heuristic

**Require:** circuit  $\mathcal{G}$

**Require:** maximum number of iterations,  $N$

- 1: partition circuit into trees
- 2: select initial values for dangling inputs
- 3: **for**  $i = 0$  to  $N$  **do**
- 4:     **for all** partitions **do**
- 5:         choose IVC and INC using dynamic programming
- 6:     **end for**
- 7:     update dangling input values
- 8:     **if** solution is the same as previous **then**
- 9:         break {Check for convergence}
- 10:    **end if**
- 11:    **if** oscillation is detected **then**
- 12:         repartition the circuit
- 13:    **end if**
- 14: **end for**
- 15: greedily remove INCs that do not affect delay
- 16: **return** input vector and INC placements

# Heuristic

**Require:** circuit  $\mathcal{G}$

**Require:** maximum number of iterations,  $N$

- 1: partition circuit into trees
- 2: select initial values for dangling inputs
- 3: **for**  $i = 0$  to  $N$  **do**
- 4:     **for all** partitions **do**
- 5:         choose IVC and INC using dynamic programming
- 6:     **end for**
- 7:     update dangling input values
- 8:     **if** solution is the same as previous **then**
- 9:         break {Check for convergence}
- 10:    **end if**
- 11:    **if** oscillation is detected **then**
- 12:         repartition the circuit
- 13:    **end if**
- 14: **end for**
- 15: greedily remove INCs that do not affect delay
- 16: **return** input vector and INC placements

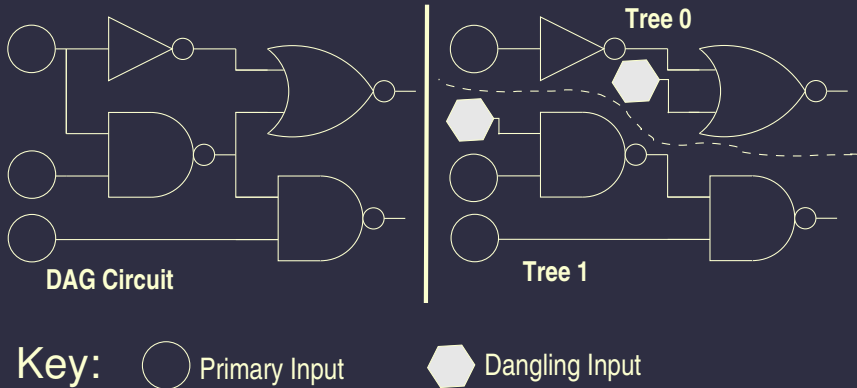
# Heuristic

**Require:** circuit  $\mathcal{G}$

**Require:** maximum number of iterations,  $N$

- 1: partition circuit into trees
- 2: select initial values for dangling inputs
- 3: **for**  $i = 0$  to  $N$  **do**
- 4:     **for all** partitions **do**
- 5:         choose IVC and INC using dynamic programming
- 6:     **end for**
- 7:     update dangling input values
- 8:     **if** solution is the same as previous **then**
- 9:         break {Check for convergence}
- 10:    **end if**
- 11:    **if** oscillation is detected **then**
- 12:         repartition the circuit
- 13:    **end if**
- 14: **end for**
- 15: greedily remove INCs that do not affect delay
- 16: **return** input vector and INC placements

# Dangling Inputs





# Partitioning

## Partitioning for Other Problems

- Proposed for other problems (e.g., leakage power minimization, tech mapping)
- Additive cost function in these cases
- Maintain large partitions

## Partitioning for INC

- Maximum cost function
- Maintain critical path in a single partition
- Keep connections with lowest slack

# Heuristic

**Require:** circuit  $\mathcal{G}$

**Require:** maximum number of iterations,  $N$

- 1: partition circuit into trees
- 2: select initial values for dangling inputs
- 3: **for**  $i = 0$  to  $N$  **do**
- 4:     **for all** partitions **do**
- 5:         choose IVC and INC using dynamic programming
- 6:     **end for**
- 7:     update dangling input values
- 8:     **if** solution is the same as previous **then**
- 9:         break {Check for convergence}
- 10:    **end if**
- 11:    **if** oscillation is detected **then**
- 12:         repartition the circuit
- 13:    **end if**
- 14: **end for**
- 15: greedily remove INCs that do not affect delay
- 16: **return** input vector and INC placements

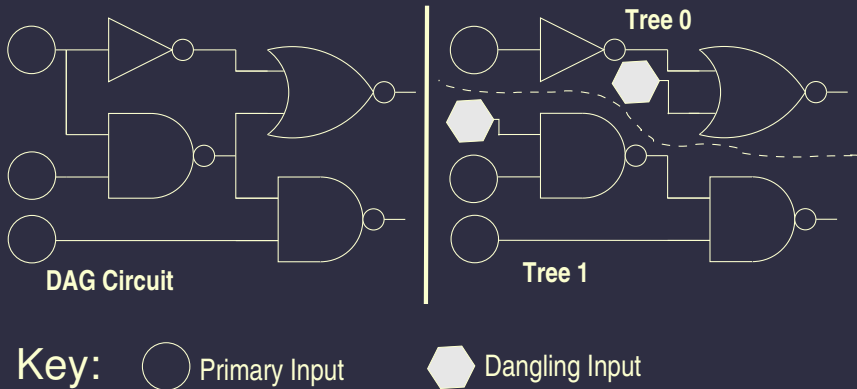
# Heuristic

**Require:** circuit  $\mathcal{G}$

**Require:** maximum number of iterations,  $N$

- 1: partition circuit into trees
- 2: select initial values for dangling inputs
- 3: **for**  $i = 0$  to  $N$  **do**
- 4:     **for all** partitions **do**
- 5:         choose IVC and INC using dynamic programming
- 6:     **end for**
- 7:     update dangling input values
- 8:     **if** solution is the same as previous **then**
- 9:         break {Check for convergence}
- 10:    **end if**
- 11:    **if** oscillation is detected **then**
- 12:         repartition the circuit
- 13:    **end if**
- 14: **end for**
- 15: greedily remove INCs that do not affect delay
- 16: **return** input vector and INC placements

# Dangling Inputs



# Initial Assignment

## Initial Assignment

- Apply dynamic programming algorithm to the full DAG circuit
- When conflicting assignments occur, choose the majority
- Choose 1 when ties occur

# Heuristic

**Require:** circuit  $\mathcal{G}$

**Require:** maximum number of iterations,  $N$

- 1: partition circuit into trees
- 2: select initial values for dangling inputs
- 3: **for**  $i = 0$  to  $N$  **do**
- 4:     **for all** partitions **do**
- 5:         choose IVC and INC using dynamic programming
- 6:     **end for**
- 7:     update dangling input values
- 8:     **if** solution is the same as previous **then**
- 9:         break {Check for convergence}
- 10:    **end if**
- 11:    **if** oscillation is detected **then**
- 12:         repartition the circuit
- 13:    **end if**
- 14: **end for**
- 15: greedily remove INCs that do not affect delay
- 16: **return** input vector and INC placements

# Heuristic

**Require:** circuit  $\mathcal{G}$

**Require:** maximum number of iterations,  $N$

- 1: partition circuit into trees
- 2: select initial values for dangling inputs
- 3: **for**  $i = 0$  to  $N$  **do**
- 4:     **for all** partitions **do**
- 5:         choose IVC and INC using dynamic programming
- 6:     **end for**
- 7:     update dangling input values
- 8:     **if** solution is the same as previous **then**
- 9:         break {Check for convergence}
- 10:    **end if**
- 11:    **if** oscillation is detected **then**
- 12:         repartition the circuit
- 13:    **end if**
- 14: **end for**
- 15: greedily remove INCs that do not affect delay
- 16: **return** input vector and INC placements

# Dynamic Programming

## Forward Pass

- Compute input combination and INC state with 0 output and minimal arrival time
- Compute input combination and INC state with 1 output and minimal arrival time

## Backward Pass

- Choose output value with minimal arrival time for output
- Back-propagate the values



# Heuristic

**Require:** circuit  $\mathcal{G}$

**Require:** maximum number of iterations,  $N$

- 1: partition circuit into trees
- 2: select initial values for dangling inputs
- 3: **for**  $i = 0$  to  $N$  **do**
- 4:     **for all** partitions **do**
- 5:         choose IVC and INC using dynamic programming
- 6:     **end for**
- 7:     update dangling input values
- 8:     **if** solution is the same as previous **then**
- 9:         break {Check for convergence}
- 10:    **end if**
- 11:    **if** oscillation is detected **then**
- 12:         repartition the circuit
- 13:    **end if**
- 14: **end for**
- 15: greedily remove INCs that do not affect delay
- 16: **return** input vector and INC placements

# Heuristic

**Require:** circuit  $\mathcal{G}$

**Require:** maximum number of iterations,  $N$

- 1: partition circuit into trees
- 2: select initial values for dangling inputs
- 3: **for**  $i = 0$  to  $N$  **do**
- 4:     **for all** partitions **do**
- 5:         choose IVC and INC using dynamic programming
- 6:     **end for**
- 7:     update dangling input values
- 8:     **if** solution is the same as previous **then**
- 9:         break {Check for convergence}
- 10:    **end if**
- 11:    **if** oscillation is detected **then**
- 12:         repartition the circuit
- 13:    **end if**
- 14: **end for**
- 15: greedily remove INCs that do not affect delay
- 16: **return** input vector and INC placements

# Heuristic

**Require:** circuit  $\mathcal{G}$

**Require:** maximum number of iterations,  $N$

- 1: partition circuit into trees
- 2: select initial values for dangling inputs
- 3: **for**  $i = 0$  to  $N$  **do**
- 4:     **for all** partitions **do**
- 5:         choose IVC and INC using dynamic programming
- 6:     **end for**
- 7:     update dangling input values
- 8:     **if** solution is the same as previous **then**
- 9:         break {Check for convergence}
- 10:    **end if**
- 11:    **if** oscillation is detected **then**
- 12:         repartition the circuit
- 13:    **end if**
- 14: **end for**
- 15: greedily remove INCs that do not affect delay
- 16: **return** input vector and INC placements

# Heuristic

**Require:** circuit  $\mathcal{G}$

**Require:** maximum number of iterations,  $N$

- 1: partition circuit into trees
- 2: select initial values for dangling inputs
- 3: **for**  $i = 0$  to  $N$  **do**
- 4:     **for all** partitions **do**
- 5:         choose IVC and INC using dynamic programming
- 6:     **end for**
- 7:     update dangling input values
- 8:     **if** solution is the same as previous **then**
- 9:         break {Check for convergence}
- 10:    **end if**
- 11:    **if** oscillation is detected **then**
- 12:         repartition the circuit
- 13:    **end if**
- 14: **end for**
- 15: greedily remove INCs that do not affect delay
- 16: **return** input vector and INC placements

# Heuristic

**Require:** circuit  $\mathcal{G}$

**Require:** maximum number of iterations,  $N$

- 1: partition circuit into trees
- 2: select initial values for dangling inputs
- 3: **for**  $i = 0$  to  $N$  **do**
- 4:     **for all** partitions **do**
- 5:         choose IVC and INC using dynamic programming
- 6:     **end for**
- 7:     update dangling input values
- 8:     **if** solution is the same as previous **then**
- 9:         break {Check for convergence}
- 10:    **end if**
- 11:    **if** oscillation is detected **then**
- 12:         repartition the circuit
- 13:    **end if**
- 14: **end for**
- 15: greedily remove INCs that do not affect delay
- 16: **return** input vector and INC placements

# Runtime

Linear in number of gates

- Partitioning – 1 topological traversal
- Dynamic programming – 2 topological traversals
- Limit the number of iterations to a small constant (e.g., 15)

## Section outline

### 4. Heuristic

Algorithm

Experimental Results

# Experimental Results

<b>Circuit</b>	<b>% Worse than Mid</b>	<b>% Worse and UB</b>	<b>Time (s)</b>
c432	0.56	0.53	1.3
c499	-0.01	-0.10	6.7
c880	0.07	0.00	2.7
c1355	0.60	0.38	5.2
c1908	0.10	0.00	3.2
c2670	0.05	0.00	11.9
c3540	0.05	-0.10	27.0
c5315	0.00	0.00	41.0



# Area Impacts

<b>Circuit</b>	<b>Total Gates</b>	<b>INC Gates</b>	<b>Original Trans.</b>	<b>INC Trans.</b>	<b>% Increase</b>
c432	159	11	636	22	3.5
c499	526	18	1836	36	2.0
c880	336	11	1306	22	1.7
c1355	480	12	1840	24	1.3
c1908	363	8	1322	16	1.2
c2670	592	13	2302	26	1.1
c3540	725	29	2966	58	2.0
c5315	1452	12	5650	24	0.4

# Summary

- Proposed Internal Node Control (INC) for reducing static NBTI degradation on idle functional units
- Showed that INC leads to an average 26.7% reduction in delay relative to IVC alone
- Proposed a linear-time heuristic that generates near optimal results quickly

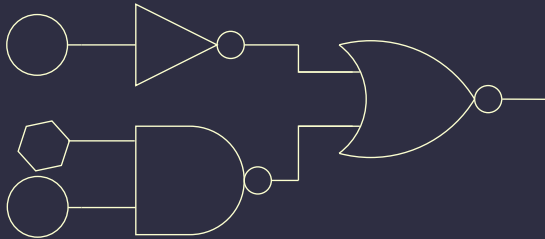
# Acknowledgments

This work was supported by the Semiconductor Research Corporation under award 2007-HJ-1593 and by the National Science Foundation under awards CCF-0702761 and CNS-0347941.

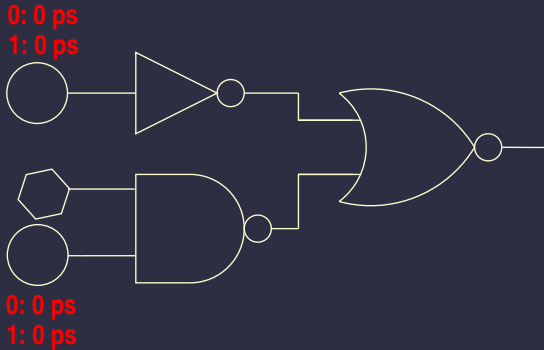
# Questions

Thank You

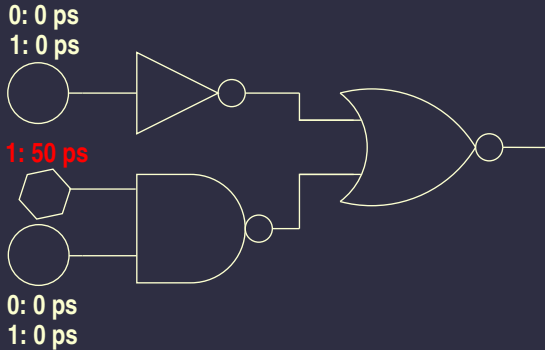
# Dynamic Programming Example



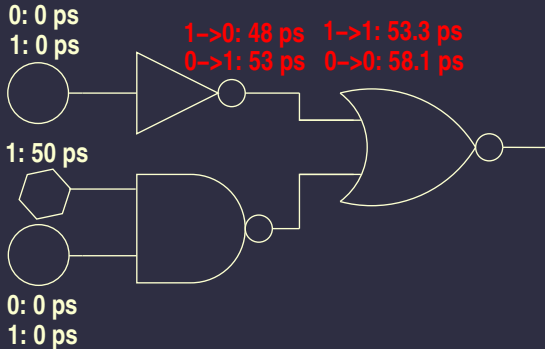
# Dynamic Programming Example



# Dynamic Programming Example

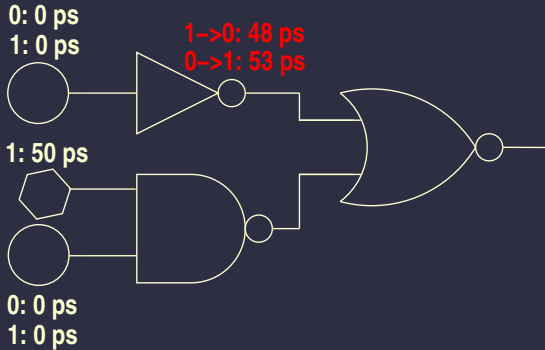


# Dynamic Programming Example

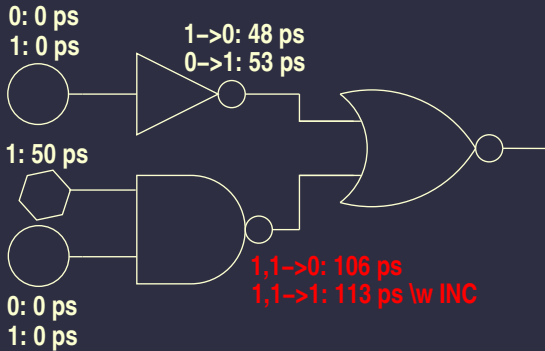




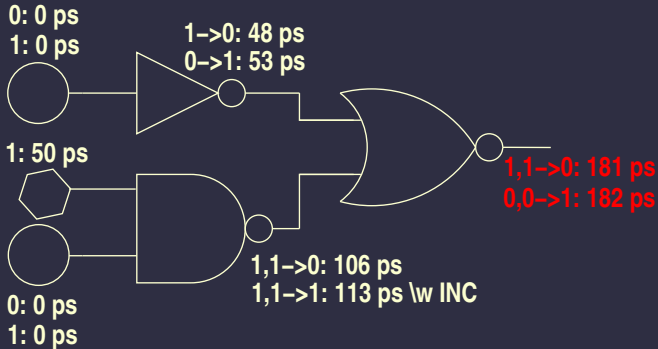
# Dynamic Programming Example



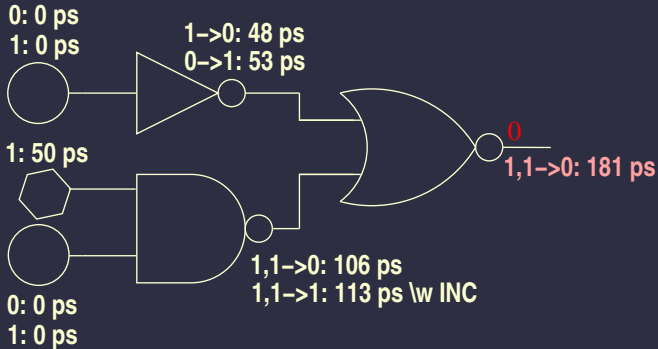
# Dynamic Programming Example



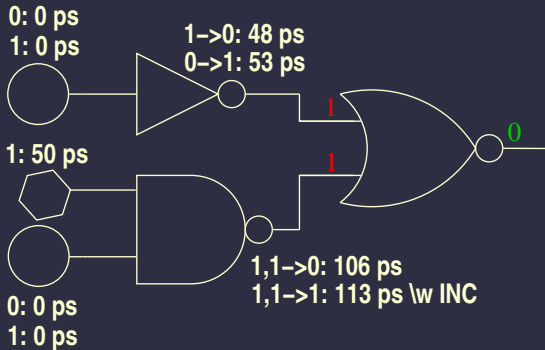
# Dynamic Programming Example



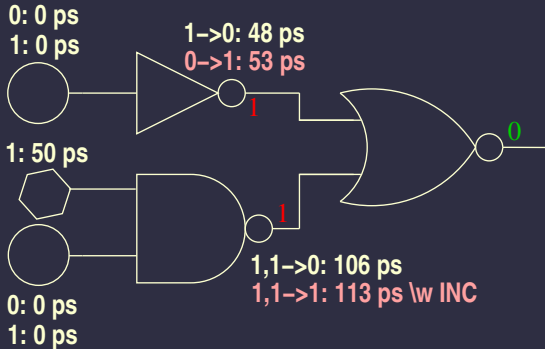
# Dynamic Programming Example



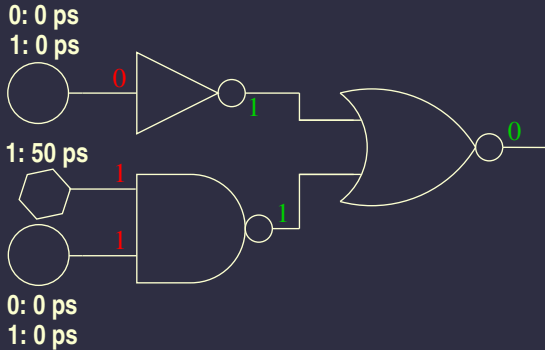
# Dynamic Programming Example



# Dynamic Programming Example



# Dynamic Programming Example



# Dynamic Programming Example

